

# TSAGAUSS

a GAUSS Library for Time Series Analysis

written / collected

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Only programs are listed here which may be used directly but auxiliary programs aren't. See the file `tsagauss.lcg` for a complete listing.

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## ACORE

- **Purpose**

Empirical autocorrelation function of time series

- **Format**

`ac = ACORE(y,nlag)`

- **Input**

`y`       $(n, k)$ -matrix,  $k$  time series of length  $n$   
`nlag`   maximum lag

- **Output**

`ac`       $(nlag + 1, k)$ -matrix, autocorrelation functions for each time series separately;  $ac[i, j] = r_{Y^{(j)}}(i - 1)$

- **Remarks**

Allowing for missing values.

For crosscorrelation function see `CCORE`

- **Source**

`tsmoment.src`

## ACORPLOT

- **Purpose**

Plot of autocorrelation function and partial correlation function  
(for up to 3 time series)

- **Format**

ACORPLOT(y,m<sub>lag</sub>,k)

- **Input**

y       $(n, k)$ -matrix, up to 3 time series, e.g.  $k \in \{1, 2, 3\}$

m<sub>lag</sub> integer, maximum lag

k      integer; if =0: no limits; if =1: with limits

- **Remarks**

For  $k = 1$ : Limits are  $2 \times \text{stdev}$  of ACF/PACF

- **Source**

tsplot.src

## ACORRB

- **Purpose**

Robust estimation of autocorrelation function by Huberizing the time series

- **Format**

`ac = ACORRB(y,nlag)`

- **Input**

`y`  $(n, 1)$ -vector, the time series

`nlag` integer, number of lags

- **Output**

`ac`  $(nlag + 1, 1)$ -vector of autocorrelation coefficients

- **Remarks**

`ac` is determined via `acovrb`; the correlations are transformed as if they were determined from correlated Gaussian variables.

- **Source**

`tsrobust.src`



## ACORTEPLOT

- **Purpose**

Plot of theoretical (and empirical) correlation / partial correlation function of time series

- **Format**

`ACORTEPLOT(a,b,x,mlag)`

- **Input**

`a`       $(p, 1)$ -vector of ar-coefficients:  $1 - \alpha_1 B - \dots - \alpha_p B^p$   
`b`       $(q, 1)$ -vector of ma-coefficients:  $1 - \beta_1 B - \dots - \beta_q B^q$   
`x`       $(n, 1)$ -vector, time series **or**  
         scalar=0: only the theoretical functions are plotted  
`mlag` integer, maximum lag

- **Source**

`tsplot.src`

## ACOVE

- **Purpose**

Empirical autocovariance function of time series

- **Format**

`ac = ACOVE(y,nlag)`

- **Input**

`y`       $(n, k)$ -matrix,  $k$  time series of length  $n$   
`nlag`   maximum lag

- **Output**

`ac`       $(nlag + 1, k)$ -matrix, autocovariance functions for each time series separately;  $ac[i, j] = c_{Y^{(j)}}(i - 1)$

- **Remarks**

Allowing missing values. For crosscovariance function see `CCOVE`

- **Source**

`tsmoment.src`

## ACOVFPER

- **Purpose**

Recovering ACF from periodogram

- **Format**

`acf = ACOVFPER(per,nlag)`

- **Input**

`per`  $(m, 1)$ -vector, periodogram at frequencies  $0 \leq k/(2n - 1) < 1/2$

`nlag` maximum ACF-lag

- **Output**

`acf`  $(nlag + 1, 1)$ -vector, ACF at lags  $0, 1, \dots, nlag$

- **Remarks**

The length  $n$  of the series is computed from the number of frequencies, i.e. the number of rows of `per`

- **Source**

`spectrum.src`

## ACOVRB

- **Purpose**

Robust estimate of autocovariance function

- **Format**

`ac = ACOVRB(y,nlag)`

- **Input**

`y`  $(n, 1)$ -vector, the time series  
`nlag` integer, number of lags

- **Output**

`ac`  $(nlag + 1, 1)$ -vector of acf-coefficients

- **Remarks**

`ac` is  $1.285 * \text{acove}(s * \text{psihub}((y - \text{tsmeanrb}(y, \&\text{psihub}))/s))$ ,  
where  $s$  is the MAD.

The constant ensures correct variance in case of a normal white noise process.

- **Source**

`tsrobust.src`

## ACOVTH

- **Purpose**

Theoretical autocovariance-function for ARMA[p,q]-process

- **Format**

`ac = ACOVTH(a,b,s,nlag)`

- **Input**

`a`       $(p, 1)$ -vector of ar-coefficients:  $\alpha_1, \dots, \alpha_p$   
`b`       $(q, 1)$ -vector of ma-coefficients:  $\beta_1, \dots, \beta_q$   
`s`      scalar, variance of error process  
`nlag` integer, number of lags

- **Output**

`ac`       $(m + 1, 1)$ -vector of acf-coefficients  $\gamma_0, \gamma_1, \dots, \gamma_{nlag}$ .

- **Reference**

McLeod, A. (1975): Derivation of the Theoretical Autocovariance Function of Autoregressive-Moving Average Time Series; Appl. Statistics, 24, 255-256

- **Remarks**

Use  $a = 0$  /  $b = 0$  for pure ma-/ar-process.

To get the autocorrelation-function, simply compute `ac/ac[1]`.

The model is assumed to be in the form

$$(1 - \alpha_1 B - \dots - \alpha_p B^p) Y_t = (1 - \beta_1 B - \dots - \beta_q B^q) \varepsilon_t$$

- **Source**

`arimafit.src`

## ARESTRB

- **Purpose**

Estimation of AR-coefficients

- **Format**

`a = AREST(y,p, meth)`

- **Input**

`y`       $(n, 1)$ -vector, time series  
`p`      integer, order of AR-model  
`meth` string for selection of the method:  
         "yw" : Yule Walker- method  
         "burg" : Burg's estimator  
         "orth" : Gram-Schmidt-orthogonalisation for partial correlations

- **Output**

`a`       $(p, 1)$ -vector of estimated AR-coefficients

- **Reference**

Newton,H.J. and Pagano,M. (1983): Computing for Autoregressions; in: Computer Science and Statistics: The Interface, J.E.Gentle (ed.), North Holland Publishing Company

- **Source**

`arimafit.src`

## ARESTRB

- **Purpose**

Robust estimation of AR[p]-model via GM-estimation

- **Format**

$\{\mathbf{a}, \text{cov}\} = \text{ARESTRB}(\mathbf{y}, p, \text{co})$

- **Input**

$\mathbf{y}$        $(n, 1)$ -vector, time series  
 $p$       integer, order of AR-model  
 $\text{co}$      flag, if  $\text{co} = 1$ , the covariance matrix of the estimates are  
         estimated via bootstrap

- **Output**

$\mathbf{a}$        $(p, 1)$ -vector of estimated AR-coefficients  
 $\text{cov}$     the estimated covarianc matrix of  $\mathbf{a}$  ( $\text{co} = 1$ )  
         or a missing value ( $\text{co} \neq 1$ )

- **Remarks**

Start values from YW-fit based on robust acf

- **Source**

`tsrobust.src`

## ARFIT

- **Purpose**

Fitting an AR[p]-model to a time series by Yule Walker method

- **Format**

$\{a, cov, aic, bic, res\} = \text{ARFIT}(y, pmax, ic, c)$

- **Input**

$y$        $(n, 1)$ -vector, time series  
 $pmax$  integer  $\geq 1$ , maximal order of AR-model  
 $ic$     string,  
         "aic": order selection by minimum aic  
         "bic": order selection by minimum bic  
 $c$       string,  
         "asyp": asymptotic covariance matrix for coefficients  
         "boot": bootstrap covariance matrix for coefficients

- **Output**

$a$        $(p, 1)$ -vector of estimated AR-coefficients  
 $cov$      $(p, p)$ -matrix, covariance matrix of coefficients  
 $aic$      $(pmax, 1)$  vector, AIC-values for all orders  $\leq pmax$   
 $bic$      $(pmax, 1)$  vector, BIC-values for all orders  $\leq pmax$   
 $res$      $(n - p, 1)$ -vector, residuals of fitted AR-model

- **Source**

arimafit.src



## ARIMAPRED

- **Purpose**

Forecasting seasonal ARIMA[p,q]x[ps,qs]-model

- **Format**

```
pred = ARIMAPRED(y,d,par,pind,psind,qind,qsind,s,lead,a)
```

- **Input**

y      ( $n, 1$ )-vector, (undifferenced) time series  
d      ( $k, 1$ )-vector, the differences which were applied to reach stationarity  
par    ( $p1 + p2 + q1 + q2, 1$ )-vector the estimated parameters of the ARIMA-model, output of armaest  
pind   ( $p1, 1$ )-vector, lags for the non seasonal ar polynom  
psind   ( $p2, 1$ )-vector, lags for the seasonal ar polynom  
qind   ( $q1, 1$ )-vector, lags for the non seasonal ma polynom  
qsind   ( $q2, 1$ )-vector, lags for the seasonal ma polynom  
s      scalar, the seasonal period  
lead   scalar, the forecasting horizon  
a      scalar, the probability  $\alpha$  to get  $(1 - \alpha)$  prediction intervals

- **Output**

pred   ( $lead, 3$ )-matrix, `pred[:,1]`: predictions  
         `pred[:,2]`: lower bounds of prediction intervals  
         `pred[:,3]`: upper bounds of prediction intervals

- **Remarks**

If an ar- or ma-polynom does not existed for estimation, the input value of the corresponding polynom must be 0.

- **Source**

`predict.src`

## ARMADHR

- **Purpose**

Estimates subset ARMA[ $p, q$ ]-model by the method of Durbin-Hannan-Rissanen.

- **Format**

$\{\text{par}, \text{stdpar}, \text{cor}, \text{e}, \text{s}\} = \text{ARMADHR}(\text{x}, \text{arsub}, \text{masub})$

- **Input**

$\text{x}$   $(n, 1)$ -vector, time series  
 $\text{arsub}$   $(p, 1)$ -vector, lags which are to be used in the autoregressive part of the model.  
or = 0 for no ar-part  
 $\text{masub}$   $(q, 1)$ -vector, lags which are to be used in the moving average part of the model.  
or = 0 for no ma-part

- **Output**

$\text{par}$   $([p + q], 1)$ -vector, the estimated parameters  
 $\text{stdpar}$   $([p + q], 1)$ -vector, estimated standard error of estimated parameters  
 $\text{cor}$   $([p + q], [p + q])$ -matrix, estimated correlation matrix of estimated parameters  
 $\text{e}$   $(n, 1)$ -vector, the estimated residuals.  
 $\text{s}$  scalar, the estimated residual variance

- **Reference**

Durbin (1960) *Revue Inst. Int. De Statist.*  
Hannan, E. J. and Rissanen, J. (1982): Recursive estimation of mixed autoregressive-moving average order; *Biometrika* 69, 81-94

- **Source**

`arimafit.src`

## ARMAEST

- **Purpose**

Maximum likelihood estimation of seasonal subset  
ARMA[p,q]x[ps,qs]-model

- **Format**

$\{\text{par}, \text{stdpar}, \text{corpar}, \text{sigma2}, \text{e}, \text{ll}\} = \text{ARMAEST}(\text{y}, \text{p}, \text{ps}, \text{q}, \text{qs}, \text{s}, \text{par0})$

- **Input**

**y**  $(n, 1)$ -vector, time series  
**p**  $(p1, 1)$ -vector, lags which are to be used in the non-seasonal  
ar part of the model  
**ps**  $(p2, 1)$ -vector, lags which are to be used in the seasonal ar  
part of the model  
**q**  $(q1, 1)$ -vector, lags which are to be used in the non-seasonal  
ma part of the model  
**qs**  $(q2, 1)$ -vector, lags which are to be used in the seasonal ma  
part of the model  
**s** scalar, the seasonal period  
**par0**  $(p1 + p2 + q1 + q2, 1)$ -vector, starting values for the parameters.  
the order of the parameters is ascending and all parameters  
of all polynoms are stacked together  
or = 0 when the program should determine starting values

- **Output**

**par**  $([p1 + p2 + q1 + q2], 1)$ -vector, the estimated parameters  
**stdpar**  $([p1 + p2 + q1 + q2], 1)$ -vector, estimated standard error of  
estimated parameters  
**cor**  $([p1 + p2 + q1 + q2], [p1 + p2 + q1 + q2])$ -matrix, estimated  
correlation matrix of estimated parameters  
**sigma2** scalar, the estimated residual variance  
**e**  $(n, 1)$ -vector, the estimated residuals.  
**ll** scalar, the value of the loglikelihood function at the estimated  
parameter values.

- **Reference**

Jones, R.H. (1980): Maximum Likelihood fitting of ARMA  
models to time series with missing observations; Technome-  
trics, 22, 389-395

- **Remarks**

If an ar or an ma- polynom is not desired, set the lags equal to 0.

The Kalman filter is used to compute the likelihood and Nelder-Mead's simplex algorithm is used as optimizer. The covariance matrix is obtained with GAUSS' procedure HESSP.

- **Source**

`armaest.src`

## ARMAMLCV

- **Purpose**

Computes asymptotic covariance matrix for  
ML estimator of ARMA[p,q]-model.

- **Format**

`v = ARMAMLCV(ar,ma)`

- **Input**

`ar`      $(p, 1)$ -vector, estimates of coefficients of ar-part  
         0 if no ar-part  
`ma`      $(q, 1)$ -vector, estimates of coefficients of ma-part  
         0 if no ma-part

- **Output**

`v`        $p+q, p+q$ )-matrix,  $n$  times the asymptotic variance-covariance  
         matrix of estimates

- **Reference**

Godolphin, E. J. and Unwin, J.M. (1983): Evaluation of the  
covariance matrix for the maximum likelihood estimator of a  
Gaussian autoregressive-moving average process; Biometrika  
70, 279-84

- **Remarks**

$v$  is determined as if the data were complete

- **Source**

`arimafit.src`

## ARMARESID

- **Purpose**

Residuals from an ARMA[p,q]-model

- **Format**

`e = ARMARESID(x,ar,ma)`

- **Input**

`x`       $(n, 1)$ -vector, time series

`ar`       $(p, 1)$ -vector the autoregressive parameters of the model

`ma`       $(q, 1)$ -vector, the moving average parameters of the model

- **Output**

`e`       $(n - \max(p, q), 1)$ -vector, the estimated residuals.

- **Source**

`regarma.src`

## ARSUBFIT

- **Purpose**

Fit of a subset-ar-model for time series (choose the lags and estimate the corresponding parameters)

- **Format**

`{arset,a,cov,res} = ARSUBFIT(y,subset,set2null,pmax)`

- **Input**

`y`         $(n, 1)$ -vector, time series  
`subset`  $(h, 1)$ -vector of lags of a given subset  
          0, no given subset  
`set2null`  $(j, 1)$ -vector of lags to be set to null  
          0, no lag is set to null  
`pmax`   integer  $ge 1$ , maximal order of ar-coefficient

- **Output**

`lagset`  $(p, 1)$ -vector, indices of relevant lags  
`a`        $(p, 1)$ -vector, estimated ar-coefficients  
`cov`     $(p, p)$ -matrix, variance matrix of estimated coefficients  
`res`     $(m, 1)$ -vector, the estimated residuals.

- **Source**

`ariamfit.src`

## BANDFILT

- **Purpose**

bandpass filtering of a time series

- **Format**

`yf = BANDFILT(y,q,l0,lc)`

- **Input**

`y`       $(n, 1)$ -vector, time series to be filtered  
`q`      scalar, gives half of length of symmetric weights  
`l0`     scalar, half the desired broadnes of the filter (in frequency terms)  
`l1`     scalar, the frequency at which the filter is centered

- **Output**

`yf`      $(n, 1)$ -vector, the filtered time series

- **Remarks**

`q` values at the begining and at the end are set to missing.

- **Source**

`linfilt.src`



## BCPLOT

- **Purpose**

Box-Cox-transformation plot for time series

- **Format**

BCPLOT(y)

- **Input**

y       $(n, 1)$ -vector, time series

- **Output**

Plot

- **Remarks**

The series is divided into 10 segments. For each segment  $i$  the mean and the standard deviation is determined. The plot shows the points  $(\ln(\text{mean}(y_i)), \ln(\text{std}(y_i)))$  together with a regression line; its slope  $b$  is given, too. The transformation  $z = y^{1-b}$  stabilizes variances.

Allowing for missing values.

- **Source**

tsplot.src

## BPLTEST

- **Purpose**

Computing the Box-Pierce-Ljung test statistic and p-values

- **Format**

`LBPTTEST(e,n,par)`

- **Input**

`e`       $(n', 2)$ -vector, the series of residuals  
`n`      scalar, length of series from which `e` is obtained  
`par`    scalar, number of parameters estimated to obtain `e`

- **Source**

`arimafit.src`

## BISPECES

- **Purpose**

Indirect bivariate spectral estimation

- **Format**

$\{f, coh, ph\} = \text{BISPECES}(y, q, \&win)$

- **Input**

$y$        $(n, 2)$ -matrix, 2 time series of length  $n$   
 $q$       scalar, number of covariances used for averaging  
 $win$     procedure, the lagwindow

- **Output**

$f$        $((n + 1)/2, 1)$ -vector of fourierfrequencies  $0, 1/n, 2/n, ..$   
 $coh$      $((n + 1)/2, 1)$ -vector, the estimated coherency at frequencies  
          $f$   
 $ph$        $((n + 1)/2, 1)$ -vector, the estimated phase at frequencies  $f$

- **Remarks**

Possible lagwindows:  
Bartlett's Lag-window: `lagwinba`  
Tukey's Lag-window: `lagwintu`  
Parzen's Lag-window: `lagwinpa`

- **Source**

`bivariat.src`

## CCORE

- **Purpose**

Computes crosscorrelation function of 2 time series

- **Format**

$\{\text{lag}, \text{cc}\} = \text{CCORE}(\mathbf{x}, \mathbf{nlag})$

- **Input**

$\mathbf{x}$        $(n, 2)$ -matrix, 2 time series of length  $n$   
 $\mathbf{nlag}$     $(2, 1)$ -vector, number of lags  $(nlag1, nlag2)$

- **Output**

$\text{lag}$     $(nlag2 - nlag2 + 1, 1)$ -vector, of lags from  $lag1$  to  $lag2$   
 $\text{cc}$      $(nlag1 - nlag2 + 1, 1)$ -vector of crosscorrelations  
 $c_{12}(\tau) / \sqrt{c_1(0) \cdot c_2(0)}$ , where  $c_{12}(\tau)$  is the crosscovariance of the two series

- **Remarks**

Allowing missing values.

- **Source**

`bivariat.src`

## CCORPLOT

- **Purpose**

Plot of crosscorrelation function for 2 time series

- **Format**

`CCORPLOT(y,mlag,lim)`

- **Input**

`y`  $(n, 2)$ -matrix, 2 time series

`mlag` integer, maximum (absolut) lag

`lim` flag, if =1, confidence limits are shown

- **Remarks**

Plotted are crosscorrelations from -mlag to +mlag.

Limits are  $2 \times \text{stdev}$  of CCF for uncorrelated series, where one is white noise.

- **Source**

`bivariat.src`

## CCOVE

- **Purpose**

Computes crosscovariance function of 2 time series

- **Format**

$\{\text{lag}, \text{cc}\} = \text{CCOVE}(\mathbf{x}, \text{nlag})$

- **Input**

$\mathbf{x}$   $(n, 2)$ -matrix, 2 time series of length  $n$

$\text{nlag}$   $(2, 1)$ -vector, range of lags  $(\text{nlag1}, \text{nlag2})$  ( $\text{nlag1} \leq \text{nlag2}$ )

- **Output**

$\text{lag}$   $(\text{nlag2} - \text{nlag1} + 1, 1)$ -vector, of lags from  $\text{lag1}$  to  $\text{lag2}$

$\text{cc}$   $(\text{nlag1} - \text{nlag1} + 1, 1)$ -vector of crosscovariances

$$\sum_{1 \leq t, t+\tau \leq n} (x_{1,t} - \bar{x}_1)(x_{2,t+\tau} - \bar{x}_2)$$

- **Remarks**

Allowing for missing values.

- **Source**

`bivariat.src`

## DIFF

- **Purpose**

Computing difference-filter of time series

- **Format**

`yd = DIFF(y,d)`

- **Input**

`y`       $(n, 1)$ -vector, time series to be differenced

`d`       $(j, 1)$ -vector, containing the lags for differencing

- **Output**

`yd`       $(n - \text{sumc}(d), 1)$ -vector, differenced series

- **Remarks**

For repeated differencing use the same lag more often.

Example:  $d = \{1, 1\}$  for simple differencing twice

- **Source**

`auxiliary.src`

## EXPOSMOOTH

- **Purpose**

Exponential smoothing of a time series, local constant model

$$y_{t+u} = m_t + \varepsilon_u, \quad -q \leq u \leq q$$

- **Format**

$\{\text{yhat}, \text{b}\} = \text{EXPOSMOOTH}(\text{y}, \text{b}, \text{start}, \text{lead})$

- **Input**

**y**  $(n, 1)$ -vector, time series

**b** scalar, smoothing constant if  $0 < \text{b} < 1$

if  $b \notin (0, 1)$  then the smoothing constant is determined to minimize the one step prediction error

**start** integer, time index from which on the one-step-predictions are given

**lead** integer, forecast horizon

- **Output**

**yhat**  $(n - \text{start} + \text{lead}, 2)$ -matrix; the first column gives the time index, and the second the one-step-forecasts

**b** scalar, smoothing constant

- **Remarks**

A plot is shown also. Use `CALL expsmooth` to see the plot only.

- **Source**

`tsdecomp.src`



## EXPOSMOOTH1

- **Purpose**

Computes exponential smoothing of time series, local linear trend model  $y_{t+u} = m_t + h \cdot u + \varepsilon_u$ ,  $-q \leq u \leq q$

- **Format**

`{yhat} = EXPOSMOOTH1(y,ab,start,lead)`

- **Input**

`y`       $(n, 1)$ -vector, time series  
`ab`       $(2, 1)$ -vector, smoothing constants ( $0 \leq ab \leq 1$ )  
             $ab[1]$  level,  $ab[2]$  slope  
`start` integer, the index from which on the one-step-predictions are determined  
`lead` integer, forecast horizon

- **Output**

`yhat`  $(n - start + lead, 2)$ -matrix; the first column gives the time index, and the second the one-step-forecasts

- **Remarks**

$h$ -step forecasts are computed as  $\hat{y}_{n,h} = \hat{m}_n + h \cdot \hat{b}_n$

- **Source**

`tsdecomp.src`

## FOURIER

- **Purpose**

Computes the fouriercoefficients of time series

- **Format**

`fc = FOURIER(y)`

- **Input**

`y`       $(n, 1)$ -vector, time series

- **Output**

`fc`       $([n/2]+1, 2)$ -matrix, the fourier coefficients at frequencies  $k/n$ ,  
 $0 \leq k/n \leq 1/2$

- **Source**

`spectrum.src`

## FOURINV

- **Purpose**

Reconstructing time series from fourier coefficients which were determined with FOURIER

- **Format**

`x = FOURINV(fcoe,n)`

- **Input**

`fcoe`  $([n/2] + 1, 2)$ -matrix, fourier coefficients at frequencies  $k/n$   
`n` integer, length of time series

- **Output**

`x`  $(n, 1)$ -vector, time series

- **Source**

`spectrum.src`

## HOLTWINT

- **Purpose**

Computes and plots exponential smoothing of time series using Holt-Winters-method

- **Format**

`yhat = HOLTWINT(y,abc,d,start,lead)`

- **Input**

`y`       $(n, 1)$ -vector, time series  
`abc`     $(3, 1)$ -vector, weights  
          `abc[, 1]`: level  
          `abc[, 2]`: ascent  
          `abc[, 3]`: seasonal component  
`d`      integer, seasonal period (1 when no seasonal component)  
`start` integer, time point from which on the forecasts are computed  
`lead` integer, forecasting horizon

- **Output**

`yhat`    $(n - start + lead, 2)$ -matrix; the first column gives the time index, and the second the one-step-forecasts

- **Remarks**

A plot of the selectet part of the series together with the one step ( $t \leq n + 1$ ) and more-step forecasts ( $n + 1 < t \leq n + h$ ) is shown also

- **Source**

`tsdecomp.src`

## IACORE

- **Purpose**

Computing the inverse autocorelation function IACF using the autocorrelation function ACF

- **Format**

`iac = IACORE(acf,m)`

- **Input**

`acf`     $(n, 1)$ -vector, acf at lags  $1, \dots, n$

`m`       integer ( $m < n$ ), maximum IACF-lag

- **Output**

`iac`     $(m, 1)$ -vector, IACF at lags  $1, \dots, m$

- **Source**

`tsmoment.src`

## INNOVREC

- **Purpose**

Estimation of MA coefficients via innovation algorithm by Brockwell & Davis

- **Format**

$\{\mathbf{th}, v\} = \text{INNOVREC}(\mathbf{x}, m)$

- **Input**

$\mathbf{x}$        $(n, 1)$ -vector, the time series

$m$       integer ( $m < n$ ), number of MA-coefficient

- **Output**

$\mathbf{th}$      $(m, 1)$ -vector, MA coefficients

$v$       scalar, estimate of the innovation variance

- **Reference**

Brockwell & Davis (1987): Time Series: Theory and Methods;  
New York: Springer

- **Source**

`arimafit.src`

## LDREC

- **Purpose**

Levinson-Durbin recursion for determining all coefficients  $a(i, j)$

- **Format**

`mat = LDREC(acf)`

- **Input**

`acf`  $(p + 1, 1)$ -vector,  
 $acov(0), \dots, acov(p)$  or  $1, acor(1), \dots, acor(p)$

- **Output**

`mat`  $(p, p + 2)$ -matrix with coefficients in lower triangular,  
pacf in the last column and  $Q(p)$  in column  $p + 1$

- **Source**

`arimafit.src`

## LINFILT

- **Purpose**

Filtering time series

- **Format**

$\{y\} = \text{LINFILT}(x, f, s)$

- **Input**

$x$        $(n, 1)$ -vector, time series  
 $f$        $(k, 1)$ -vector, filter weights  
 $s$       scalar, time shift of output

- **Output**

$y$       filtered time series

- **Remarks**

The output is  $y_{t+s} = x_t f_1 + x_{t-1} f_2 + \cdots + x_{t+1-k} f_k$ .

Suitable numbers of missings are padded at the begin or the end.

$y$  can be longer than  $x$  because of the time shift into the future ( $s > 0$ ).

- **Source**

`linfilt.src`



## MACOEFF

- **Purpose**

Computes coefficients of MA[ $\infty$ ] representation of ARMA[ $p, q$ ] process for lags 1 to  $m$ .

- **Format**

`c = MACOEFF(a,b,m)`

- **Input**

a       $(p, 1)$ -vector of ar-coefficients:  $1 - \alpha_1 B - \dots - \alpha_p B^p$   
b       $(q, 1)$ -vector of ma-coefficients:  $1 - \beta_1 B - \dots - \beta_q B^q$

- **Output**

c       $(m, 1)$ -vector, ma-coefficients:  $1 - \beta_1^* B - \dots - \beta_m^* B^m$

- **Reference**

McLeod, I. (1975): Derivation of the Theoretical Autocovariance Function of Autoregressive-Moving Average Time Series, Applied Statistics, 24, 255-256

- **Source**

`ariamfit.src`

## MAD

- **Purpose**

Computes robust scale estimator MAD for univariate samples

- **Format**

`m = MAD(x)`

- **Input**

`x`       $(n, 1)$ -vector

- **Output**

`m`      scalar, estimated MAD

- **Remarks**

$m = 1.4826 \cdot \text{med}\{|x_j - \text{med}\{x_i : 1 \leq i \leq n\}| : 1 \leq j \leq n\}$

The factor makes it an unbiased estimator of  $\sigma_X$  in a Gaussian white noise process.

- **Source**

`auxiliary.src`

## MISSAR

- **Purpose**

Interpolation of missing values in a time series by substituting them with the expected values of AR-models

- **Format**

$\{a, y\} = \text{MISSAR}(x, p)$

- **Input**

$x$        $(n, 1)$ -vector, time series with missing values

$p$       integer, maximal order of the ar-models to be used ( $p < 18$ )

- **Output**

$a$        $(p, p)$ -matrix, the estimated ar-coefficients for the models up to order  $p$

$y$        $(n, 1)$ -vector, filled time series

- **Reference**

Miller, R.B. and Ferreiro, O.M. (1984): A strategy to complete a time series with missing observations; In: E. Parzen (ed.): Time series analysis of irregularly observed data; Berlin: Springer

- **Remarks**

There must not be missing values at the beginning and the end of the series.

Set `_iterout_=1` to watch iteration history.

- **Source**

`missfilll.src`

## MISSLS

- **Purpose**

Minimum mean square error interpolation of missing values

- **Format**

`y = MISSLS(x,tol,theo,p)`

- **Input**

`x`       $(n, 1)$ -vector, time series with missing values  
`tol`    scalar, control stopping criterion,  
         minimum absolut change in parameter  
`theo`   theoretical IACF for interpoltation, or  
         0, for interpolation with estimated IACF  
`p`      estimation of IACF with parameter of AR[ $p$ ]-Modell  
         0, choosing  $p = n/10$

- **Output**

`y`       $(n, 1)$ -vector, filled time series

- **Reference**

Brubacker, S. and Wilson, G. (1976): Interpolating time series with applications to the estimation of holiday effects on electricity demand; Journal of the Royal Statistical Society, C, 25, 107-116

- **Remarks**

There must not be missing values at the beginning and the end of the series.

- **Source**

`missfilll.src`

## OUTIDENTIFY

- **Purpose**

Iterative procedure to identify impact, locations and type of outliers in ar processes

- **Format**

`{alpha, aus, sigma2} = OUTIDENTIFY(y, p, k)`

- **Input**

`y`       $(n, 1)$ -vector, time series  
`p`      scalar, the order of ar model  
`k`      scalar, the level of the tests for deciding which value is to be considered an outlier.

- **Output**

`alpha`  $(p, 1)$ -vector, the ar coefficients  
`aus`    $(k, 3)$ -matrix with information about outliers:  
      `aus[., 1]` = type of outlier 1 = ao, 2=io  
      `aus[., 2]` = impact  
      `aus[., 3]` = time points where outliers were detected  
`sigma2` estimated residual variance

- **Reference**

Wei, W.W.S.(1990): Time Series Analysis, Univariate and Multivariate Methods; Redwood City: Addison Wesley see also: Chang and Tiao (1983)

- **Source**

`tsmoment.src`

## PACFE

- **Purpose**

Partial autocorrelation function

- **Format**

`pa = PACFE(y,m,meth)`

- **Input**

`y`       $(n, 1)$ -vector, time series

`m`      scalar, maximum lag

`meth` string, the method :

    "burg": Burg's algorithm

    "orth": Orthogonalization

    otherwise: Levinson Durbin recursion is used

- **Output**

`pa`       $(m, 1)$ -vector, pacf

- **Reference**

Newton,H.J. and Pagano,M. (1983): Computing for Autoregressions; in: Computer Science and Statistics: The Interface, J.E.Gentle (ed.), North Holland Publishing Company

- **Source**

`tsmoment.src`

## PERIOD01

- **Purpose**

Determines the periodogram of centered time series at given frequencies

- **Format**

`per = PERIOD01(y,freq,c)`

- **Input**

`y`  $(n, 1)$ -vector, time series

`freq`  $(k, 1)$ -vector, frequencies

`c` scalar; if `c=1`, with mean correction, else no mean correction

- **Output**

`per`  $(k, 1)$ -vector, periodogram

- **Source**

`spectrum.src`

## PERIOD02

- **Purpose**

Determines the periodogram of centered time series at equally spaced frequencies

- **Format**

$\{\text{per}, \text{f}\} = \text{PERIOD02}(\text{y}, \text{nfreq})$

- **Input**

$\text{y}$   $(n, 1)$ -vector, time series

$\text{nfreq}$  integer, the number of equally spaced frequencies

- **Output**

$\text{per}$   $(\text{nfreq}, 1)$ -vector, periodogram at frequencies  $k/(2 \cdot \text{nfreq} - 1)$

$\text{f}$   $(\text{nfreq}, 1)$ -vector, frequencies

- **Source**

`spectrum.src`



## PERIOD03

- **Purpose**

Determines the periodogram at given frequencies using the `acf`

- **Format**

`per = PERIOD03(acf,freq)`

- **Input**

`acf`  $(m+1, 1)$ -vector, acf at lags  $0, 1, \dots, m$

`freq`  $(k, 1)$ -vector, frequencies

- **Output**

`per`  $(k, 1)$ -vector, periodogram

- **Remarks**

Use `freq=sega(0,1/(2*n-1),n)` to be able to recover the autocovariancefunction by `acovfper`.

- **Source**

`spectrum.src`

## PERIOD04

- **Purpose**

Determines the periodogram at equally spaced frequencies using the acf

- **Format**

$\{\text{per}, \text{f}\} = \text{PERIOD03}(\text{acf}, \text{nf})$

- **Input**

acf     $(m, 1)$ -vector, acf at lags  $0, 1, \dots, m - 1$

nf     integer, the number of frequencies

- **Output**

per     $(nf + 1, 1)$ -vector, periodogram at frequencies  $f$

f        $(nf + 1, 1)$ -vector, frequencies  $k/(2n_f), k = 0, 1, \dots, n_f$

- **Remarks**

Using  $m < n$  where  $n$  is the length of the series is equal to perform spectral estimation with Daniell window.

Use **nf=n** with series length  $n$  to be able to recover the autocovariancefunction by **acovfper** .

- **Source**

spectrum.src

## PERIODORB

- **Purpose**

Robust determination of periodogram at equally spaced frequencies using regression interpretation

- **Format**

$\{f, p\} = \text{PERIODORB}(y, \psi)$

- **Input**

$y$        $(n, 1)$ -vector, th time series  
 $\psi$      $\psi$ -function

- **Output**

$f$        $([n/2] + 1, 1)$ -vector, fourier frequencies  
 $p$        $([n/2] + 1, 1)$ -vector, periodogram at fourier frequencies

- **Remarks**

For Fourier frequencies  $\lambda$  the LS-approach  $\sum [(y_t - \bar{y}) - b_1 \cos(2\pi\lambda t) - b_2 \sin(2\pi\lambda t)]^2 \stackrel{!}{=} \min$  leads to solutions  $\hat{b}_1, \hat{b}_2$  which satisfy  $I(\lambda) = \frac{n}{4}[\hat{b}_1^2 + \hat{b}_2^2]$  where  $I(\lambda)$  is the periodogram. In this procedure the mean is replaced by a m-estimate and the ls-regression by m-estimation.

- **Source**

`tsrobust.src`

## RANDAR

- **Purpose**

Simulates a realisation of a Gaussian AR[p]-process

- **Format**

`x = RANDAR(a,s,n)`

- **Input**

`a`       $(p, 1)$ -vector of AR-coefficients:  $1 - \alpha_1 B - \dots - \alpha_p B^p$   
`s`      scalar, variance of error process  
`n`      integer, length of time series

- **Output**

`x`       $(n, 1)$ -vector, time series

- **Reference**

McLeod, I. A. and Hipel, K. W. (1978): Simulation Procedures for Box-Jenkins Models; Water Resources Research 14, 969-975

- **Source**

`tssim.src`

## RANDARMA

- **Purpose**

Simulates a realisation of a Gaussian ARMA[p,q]-process

- **Format**

`x = RANDARMA(a,b,s,n)`

- **Input**

`a`       $(p, 1)$ -vector of ar-coefficients:  $1 - \alpha_1 B - \dots - \alpha_p B^p$   
`b`       $(q, 1)$ -vector of ma-coefficients:  $1 - \beta_1 B - \dots - \beta_q B^q$   
`s`      scalar, variance of error process  
`n`      integer, length of time series

- **Output**

`x`       $(n, 1)$ -vector, time series

- **Reference**

McLeod, I. A. and Hipel, K. W. (1978): Simulation Procedures for Box-Jenkins Models; Water Resources Research 14, 969-975

- **Source**

`tssim.src`

## REGAR

- **Purpose**

Approximative maximum likelihood estimation of a regression with AR[p]-errors

- **Format**

$\{\mathbf{b}, \mathbf{a}, \text{stdb}, \text{stda}, \text{corb}, \text{cora}, \mathbf{s}\} = \text{REGAR}(\mathbf{y}, \mathbf{x}, p)$

- **Input**

$\mathbf{y}$        $(n, 1)$ -vector, the (dependent) time series  
 $\mathbf{x}$        $(n, m)$ -matrix of regressors or scalar  
          =1 for constant, =0 without constant  
 $p$       scalar, order of ar-model

- **Output**

$\mathbf{b}$        $(m, 1)$ -vector, regression-coefficients  
 $\mathbf{a}$        $(p, 1)$ -vector, ar-coefficients  
 $\text{stdb}$   $(m, 1)$ -vector, standard deviations of  $\mathbf{b}$   
 $\text{stda}$   $(p, 1)$ -vector, standard deviations of  $\mathbf{a}$   
 $\text{corb}$   $(m, m)$ -matrix, the correlation matrix of  $\mathbf{b}$   
 $\text{cora}$   $(p, p)$ -matrix, the correlation matrix of  $\mathbf{a}$   
 $\mathbf{s}$       scalar, error variance

- **Reference**

Fuller, W.A. (1996): Introduction to statistical time series;  
New York: Wiley  
Brockwell, P.J. and Davis, R.A. (1987): Time series: theory  
and methods; New York: Springer

- **Remarks**

The model is  $y_t = \mathbf{x}_t' \boldsymbol{\beta} + z_t$ ,  $t = 1, \dots, n$  where  $z_t = \sum_{j=1}^p \alpha_j z_{t-j} + \epsilon_t$   
The solution is found by iterative generalized least squares.  
Gram-Schmid orthogonalization is used to obtain GLS estimates of beta.  
 $\mathbf{b}$  and  $\mathbf{a}$  are asymptotically uncorrelated.  
Set `_iterout_=1` to watch iteration history

- **Source**

`regar.src`

## REGARMA

- **Purpose**

Maximum likelihood estimation of a regression model with ARMA[p,q]-errors

- **Format**

$\{\mathbf{b}, \mathbf{a}, \mathbf{th}, \mathbf{stdb}, \mathbf{stda}, \mathbf{stdth}, \mathbf{corb}, \mathbf{cora}, \mathbf{s}\} = \text{REGARMA}(\mathbf{y}, \mathbf{x}, \mathbf{p}, \mathbf{q})$

- **Input**

$\mathbf{y}$        $(n, 1)$ -vector, the (dependent) time series  
 $\mathbf{x}$        $(n, m)$ -matrix of regressors or scalar  
           =1 for constant, =0 without constant  
 $\mathbf{p}$       scalar, the order of the ar-polynom  
 $\mathbf{q}$       scalar, the order of the ma-polynom

- **Output**

$\mathbf{b}$        $(m, 1)$ -vector, regression-coefficients  
 $\mathbf{a}$        $(p, 1)$ -vector, ar-coefficients  
 $\mathbf{th}$       $(q, 1)$ -vector, ma-coefficients  
 $\mathbf{stdb}$   $(m, 1)$ -vector, standard deviations of  $\mathbf{b}$   
 $\mathbf{stda}$   $(p, 1)$ -vector, standard deviations of  $\mathbf{a}$   
 $\mathbf{stdth}$   $(q, 1)$ -vector, standard deviations of  $\mathbf{th}$   
 $\mathbf{corb}$   $(m, m)$ -matrix, the covariance matrix of  $\mathbf{b}$   
 $\mathbf{cora}$   $(p + q, p + q)$ -matrix, the covariance matrix of  $(\mathbf{a}, \mathbf{th})$   
 $\mathbf{s}$       scalar, error variance

- **Reference**

M. A. Wincek and G.C. Reinsel (1986): An exact maximum likelihood estimation procedure for regression-ARMA time series models with possibly nonconsecutive data; J. R. Statist. Soc. B, 48, 303-313

- **Remarks**

The model is  $y_{t_i} = \mathbf{x}'_{t_i} \boldsymbol{\beta} + z_{t_i}$ ,  $i = 1, \dots, n$  where  $t_1 < t_2 < \dots < t_n$  and  $z_t = \sum_{j=1}^p \alpha_j z_{t-j} + \epsilon_t - \sum_{j=1}^q \theta_j \epsilon_{t-j}$

The initial values are computed via the method by Durbin-Hannan-Rissanen .

The algorithm is likely to diverge when the starting values do not belong to a stationary and invertible model or when the model is grossly misspecified.

$\mathbf{b}$  and  $(\mathbf{a}, \mathbf{th})$  are asymptotically uncorrelated.

Set `_iterout_=1` to watch iteration history

- Source

`regarma.src`



## ROOTCHECK

- **Purpose**

Computing the norms of the roots of  $1 - a_1z - \dots - a_pz^p = 0$

- **Format**

`r = ROOTCHECK(a)`

- **Input**

`a`       $(p, 1)$ -vector, coefficients  $a_1, a_2, \dots, a_p$

- **Output**

`r`       $(p, 1)$ -vector, norms of the roots

- **Remarks**

Non existing coefficients in  $a$  must be set to zero.

- **Source**

`arimafit.src`

## RUNMEAN

- **Purpose**

Time series smoothing by simple moving averages

- **Format**

`g = RUNMEAN(y, q)`

- **Input**

`y`       $(n, 1)$ -vector, time series to be smoothed  
`q`      integer, span of moving average

- **Output**

`g`       $(n, 1)$ -vector, smooth component

- **Remarks**

Ends are filled with missings.

- **Source**

`tsdecomp.src`

## RUNMED

- **Purpose**

Time series smoothing by moving median

- **Format**

`g = RUNMED(y, q)`

- **Input**

`y`       $(n, 1)$ -vector, time series to be smoothed

`q`      integer, span of moving median;  $q$  must be odd.

- **Output**

`g`       $(n, 1)$ -vector, smooth component

- **Remarks**

Ends are filled with missings.

- **Source**

`tsdecomp.src`

## SEASUBPLOT

- **Purpose**

Plot of seasonal subseries

- **Format**

SEASUBPLOT(y,d)

- **Input**

y       $(n, 1)$ -vector, the time series  
d      integer, seasonal period

- **Remarks**

For the seasonal subseries  $y_i, y_{i+d}, y_{i+2d}, \dots$  the means and the corresponding values are shown.

$y$  may also be the smooth component + seasonal component or the pure seasonal component of a time series.

If  $y$  is the pure seasonal component the means should approximately be equal to zero.

- **Source**

tsplot.src

## SIGN

- **Purpose**

Sign of numeric variables

- **Format**

$y = \text{SIGN}(x)$

- **Input**

$x$        $(n, k)$ -matrix

- **Output**

$y$        $(n, k)$ -matrix, consisting of -1's and 1's

- **Source**

`auxiliary.src`

## SMOOTHLS

- **Purpose**

Smoothing of time series by least square spline

- **Format**

`g = SMOOTHLS(y,beta)`

- **Input**

`y`       $(n, 1)$ -vector, time series  
`beta` scalar, smoothing parameter

- **Output**

`g`       $(n, 1)$ -vector, smooth component

- **Remarks**

The bigger *beta* is, the smoother *g* will be.  
This smoothing spline is sometimes called Hodrick-Prescott filter.

- **Source**

`tsdecomp.src`

## SMOOTHRB

- **Purpose**

Smoothing of time series by robust spline

- **Format**

`g = SMOOTHRB(y,beta,&psi)`

- **Input**

`y`       $(n, 1)$ -vector, time series  
`beta`   scalar, smoothing parameter  
`&psi`   function, psi-function

- **Output**

`g`       $(n, 1)$ -vector, smooting component

- **Reference**

For the psi functions see Spaeth, H. (1987): Mathematische Software zur linearen Regression, p.198, Munich, Oldenbourg

- **Remarks**

The bigger *beta* is, the smoother *g* will be.

Possible psi-functions:

`psibiw`, `psihamp`, `psihub`, `psifair`, `psithg`

- **Source**

`tsrobust.src`

## SPECARMA

- **Purpose**

Computes the theoretical spectrum of an ARMA[p,q]-process

- **Format**

$\{\text{sp}, \text{fr}\} = \text{SPECARMA}(\text{a}, \text{b}, \text{s}, \text{n})$

- **Input**

**a**       $(p, 1)$ -vector of ar-coefficients:  $1 - \alpha_1 B - \dots - \alpha_p B^p$   
**b**       $(q, 1)$ -vector of ma-coefficients:  $1 - \beta_1 B - \dots - \beta_q B^q$   
**s**      scalar, variance of error process  
**n**      integer, the number of equally spaced frequencies

- **Output**

**sp**     $(n + 1, 1)$ -vector, spectrum  
**fr**     $(n + 1, 1)$ -vector, frequencies

- **Source**

`spectrum.src`



## SPECESTAR

- **Purpose**

Autoregressive spectral estimation with simultaneous confidence bands

- **Format**

$\{s, \text{bound}, f\} = \text{SPECESTAR}(y, p, nf, \text{conf})$

- **Input**

$y$        $(n, 1)$ -vector, time series  
 $p$       scalar, order of ar-model used for the estimation  
 $nf$      scalar, number of equally spaced frequencies where the spectrum is estimated  
 $\text{conf}$  scalar, the level for the confidence bounds

- **Output**

$s$        $(nf + 1, 1)$ -vector, estimated spectrum  
 $\text{bound}$   $(nf + 1, 2)$ -matrix, confidence bounds for the spectrum  
 $f$        $(nf + 1, 1)$ -vector, frequencies

- **Reference**

Newton, H.J. and Pagano, M. (1984): Simultaneous confidence bands for autoregressive spectra; *Biometrika*, 71, 197-202

Newton, H.J. (1988): Timeslab, a time series laboratory; Belmont, CA. : Wadsworth & Brooks/Cole

- **Remarks**

If no bounds are desired, set `conf` equal to 0.

The series needs to be rather long for the upper bounds to be finite (otherwise the upperbound is set missing).

- **Source**

`spectrum.src`

## SPECESTD

- **Purpose**

Direct spectral estimation of time series using periodogram window

- **Format**

$\{s, f\} = \text{SPECESTD}(y, e, \&\text{wind}, \text{conf})$

- **Input**

$y$        $(n, 1)$ -vector, time series  
 $e$       scalar, equal bandwidth,  $e$  must be  $0 \leq e < 0.5$   
 $\text{wind}$    function, periodogram window  
 $\text{conf}$    scalar, the level for confidence intervals

- **Output**

$s$        $([n/2]+1, 3)$ -matrix, estimated spectrum at fourier frequencies  
          $0, 1/n, \dots$  with lower and upper confidence limits  
 $f$        $([n/2] + 1, 1)$ -vector, frequencies

- **Remarks**

Possible periodogram windows:

Bartlett's window: `perwinba`

Parzen's window: `perwinpa`

Tukey's window: `perwintu`

truncated periodogram window: `perwintp`

- **Source**

`spectrum.src`

## SPECESTI

- **Purpose**

Indirect spectral estimation of time series using lag window

- **Format**

$\{s, f\} = \text{SPECESTI}(y, q, \&\text{wind})$

- **Input**

$y$   $(n, 1)$ -vector, time series

$q$  integer, number of covariances used for averaging

$\text{wind}$  function, lag window

- **Output**

$s$   $([n/2] + 1, 1)$ -vector, estimated spectrum at fourierfrequencies  
 $0, 1/n, \dots, [n/2]/n$

$f$   $([n/2] + 1, 1)$ -vector, frequencies

- **Remarks**

Possible lag windows:

Bartlett's window: `lagwinba`

Parzen's window: `lagwinpa`

Tukey's window: `lagwintu`

- **Source**

`spectrum.src`

## SPLINEDECOMP

- **Purpose**

Spline decomposition of a time series

- **Format**

$\{g, s\} = \text{SPLINEDECOMP}(x, d, \alpha, \beta)$

- **Input**

$x$        $(n, 1)$ -vector, time series  
 $d$       integer, seasonal period  
 $\alpha$  scalar, weight for smooth component  
 $\beta$  scalar, weight for seasonal component

- **Output**

$g$        $(n, 1)$ -vector, smooth component  
 $s$        $(n, 1)$ -vector, seasonal component

- **Source**

`tsdecomp.src`

## SYMPLOT

- **Purpose**

Symmetry plot of time series

- **Format**

SYMPLOT(x)

- **Input**

x       $(n, 1)$ -vector, time series

- **Source**

tsplot.src

## TAKE

- **Purpose**

Selecting the first or last rows of a matrix

- **Format**

`ys = TAKE(y, q)`

- **Input**

`y`       $(n, k)$ -matrix  
`q`      integer, number of rows to be taken out of `y`  
          $q > 0$ , the first `q` rows are taken  
          $q == 0$ , an empty vector is returned  
          $q < 0$ , the last `q` rows are taken

- **Output**

`ys`       $(q, k)$ -matrix, consisting of the selected rows

- **Remarks**

If  $|q| \geq n$ , then  $ys = y$ .

- **Source**

`auxiliary.src`

## TAPER

- **Purpose**

Tapermodification of a time series using a cosinus-taper

- **Format**

`z = TAPER(y,part)`

- **Input**

`y`       $(n, 1)$ -vector, time series

`part` scalar, part of time series to be modified

- **Output**

`z`       $(n, 1)$ -vector, modified time series

- **Remarks**

Part must be  $0 \leq part \leq 0.5$

- **Source**

`linfilt.src`

## TRENDEXTRAPOL

- **Purpose**

Trendextrapolation of a time series

- **Format**

$\{\text{pred}, \text{low}, \text{up}, \text{beta}\} = \text{TRENDEXTRAPOL}(\text{y}, \text{p}, \text{alpha}, \text{lead})$

- **Input**

$\text{y}$   $(n, 1)$ -vector, time series

$\text{p}$  scalar, the order of the trend polynom

$\text{alpha}$  probability to determine  $(1 - \alpha)$ -prediction intervals

$\text{lead}$  scalar, prediction horizon

- **Output**

$\text{pred}$   $(\text{lead}, 1)$ -vector, the forecaste for time points  $n+1, \dots, n+\text{lead}$

$\text{low}$   $(\text{lead}, 1)$ -vector, lower bounds of prediction intervals

$\text{up}$   $(\text{lead}, 1)$ -vector, upper bounds of prediction intervals

$\text{beta}$   $(p + 1, 1)$  vector, the estimated coefficients for  $t^0, t^1, \dots, t^p$

- **Remarks**

The errors are assumed to be white noise

- **Source**

`predict.src`



## TSLOESS

- **Purpose**

Robust smoothing by of time series with LOESS

- **Format**

$\{\mathbf{t}, \mathbf{yhat}\} = \text{TSLOESS}(\mathbf{y})$

- **Input**

$\mathbf{y}$   $(n, 1)$ -vector, the time series

- **Output**

$\mathbf{t}$   $(n, 1)$ -vector of time indices  $(1, 2, 3, \dots, n)$

$\mathbf{yhat}$   $(n, 1)$ -vector, robustly estimated smooth component

- **Remarks**

The procedure uses the GAUSS procedure LOESS;  
missing values are allowed

- **Source**

`tsrobust.src`

## TSMEAN

- **Purpose**

Computes mean values of time series

- **Format**

`m = TSMEAN(x)`

- **Input**

`x`  $(n, k)$ -matrix,  $k$  time series of length  $n$

- **Output**

`m`  $(k, 1)$ -vector, mean values

- **Remarks**

Allowing missing values.

Means are determined via the formula  
`MEANC(y-MEANC(y))+MEANC(y)` to achieve greater accuracy.

- **Source**

`tsmoment.src`

## TSMEANRB

- **Purpose**

M-estimation of location parameter by iteratively reweighted least squares

- **Format**

`m = TSMEANRB(x,&psi)`

- **Input**

`x`         $(n, 1)$ -vector, the time series  
`psi`    psi-function

- **Output**

`m`        scalar, robustly estimated level

- **Reference**

H.Spaeth: Mathematische Software zur linearen Regression,  
p.198

- **Remarks**

Possible    psi-functions:    `psibiw`, `psihamp`, `psihub`,  
`psifair`, `psithg`

- **Source**

`tsrobust.src`

## TSMEDIAN

- **Purpose**

Computes median of time series

- **Format**

$m = \text{TSMEDIAN}(y)$

- **Input**

$y$   $(n, k)$ -matrix,  $k$  time series of length  $n$

- **Output**

$m$   $(k, 1)$ -vector, median values

- **Remarks**

Allowing missing values.

Missings are eliminated before **MEDIAN** is called. This gives more adequate results.

- **Source**

`tsmoment.src`

## TSPLIT

- **Purpose**

Plot of time series

- **Format**

TSPLIT(*y*,*step*,*start*)

- **Input**

*y*      (*n*,*p*)-matrix, *k* time series of length *n*

*step*   string, the period of the time series:

      "year", "quart", "month"

      other periodicities are displayed as label only

*start*   integer, giving the start value of the time

*step* = "year": start must be of the form yy or yyyy

*step* = "quart": start must be of the form qyy

*step* = "month": start must be of the form myy or mmyy

- **Remarks**

The first column of *y* will be used to determine the ticmarks of the abscissa

- **Source**

tsplot.src

## TSPL0T1

- **Purpose**

Plot of a time serie with optimization of viewratio

- **Format**

TSPL0T1(x)

- **Input**

x         $(n, 1)$ -vector, time series

- **Reference**

Cleveland, W.S. (1993): A model for studying display methods of statistical graphics; J. Comp. Graph. Statistics, 2, 323-343

- **Remarks**

The plot is scaled in a way that the mean angel of ascent / decent is aproximately  $45^o$

- **Source**

tsplot.src

## TSVAR

- **Purpose**

Computes variance of time series

- **Format**

$s = \text{TSVAR}(y)$

- **Input**

$y$   $(n, k)$ -matrix,  $k$  time series of length  $n$

- **Output**

$s$   $(k, 1)$ -vector, the variances

- **Remarks**

Allowing missing values.

Variances are determined via the formula  $\sum (y_i - \bar{y})^2 / (n - 1)$

- **Source**

`tsmoment.src`

## VARDIFF

- **Purpose**

computing a table of variance ratios for determining the proper orders of differencing of a time series to reach stationarity

- **Format**

VARDIFF(y,s)

- **Input**

y       $(n, 1)$ -vector, time series  
s      integer, seasonal period

- **Output**

Print of a table of variance ratios

- **Remarks**

Allowing missing values.

Table gives  $\widehat{\text{var}}((1-B)^d(1-B^s)^D y_t) / \widehat{\text{var}}(y_t)$  for  $0 \leq d, D \leq 3$

- **Source**

tsmoment.src



## VARIOGRAM

- **Purpose**

Variogram for unequal spaced time series

- **Format**

`v = VARIOGRAM(y,mlag,tol)`

- **Input**

`y`  $(n, 2)$ -matrix, the time points (first column) and values of time series (second column)

`mlag` integer, maximal time distance for variogram

`tol` scalar, window width over which the values are averaged

- **Output**

`v`  $(k, 2)$ -matrix, lags (first column) and variogram (second column)

- **Reference**

Diggle, P.J. (1990): Time Series; Oxford: Clarendon Press

- **Source**

`tsmoment.src`

## VECCORE

- **Purpose**

Computes vectorcorrelations with bootstrap standard deviations

- **Format**

$\{\text{vec}, \text{st}\} = \text{VECCORRE}(\mathbf{y}, p, q)$

- **Input**

$\mathbf{y}$        $(n, 1)$ -vector, the time series  
 $p$       integer, maximal order of AR-part  
 $q$       integer, maximal order of MA-part

- **Output**

$\text{vec}$      $(p + 1, q + 1)$ -matrix, vectorcorrelations  
 $\text{st}$      $(p + 1, q + 1)$ -matrix, standard deviations

- **Reference**

Paparoditis, E. (1990): Vektorautokorrelationen stochastischer Prozesse und die Spezifikation von ARMA-Modellen; Heidelberg: Physica-Verlag

Paparoditis, E. and B.H.J. Streitberg (1991): Order identification statistics in stationary autoregressive-moving average models: vector autocorrelations and the bootstrap; Journal of Time Series Analysis 13, 415-434

- **Remarks**

Additionally a table of the vectorcorrelations is printed; the entries are marked, where the confidence intervals  $\text{vec}_{i,j} \pm 2 \cdot \text{st}_{i,j}$  do not contain zero.

- **Source**

`tsmoment.src`

## WNTEST

- **Purpose**

Graphical white noise test for a time series or a series of regression residuals

- **Format**

`WNTEST(e,alpha,k)`

- **Input**

`e`         $(n, 1)$ -vector, the time series or residuals  
`alpha` scalar, level of significance  
`k`        integer, number of regressors

- **Output**

A plot is drawn.

- **Remarks**

If  $k = 0$ ,  $e$  is interpreted as time series without regressors  
The Kolmogorov test by Bartlett/Durbin with residuals accepts randomness when the cumulative periodogram remains inside the inner boundary. The test rejects this hypothesis when the periodogram crosses the outer boundary. Otherwise it is inconclusive.

- **Source**

`spectrum.src`